

# TESTS OF THE ELECTROWEAK THEORY AT HERA

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1.

INTRODUCTION

HERA :  $e_{\lambda}^{\pm} p$  - COLLISIONS

H1, ZEUS

$$\sqrt{s} = 134 \dots \underline{314} \text{ GeV}$$

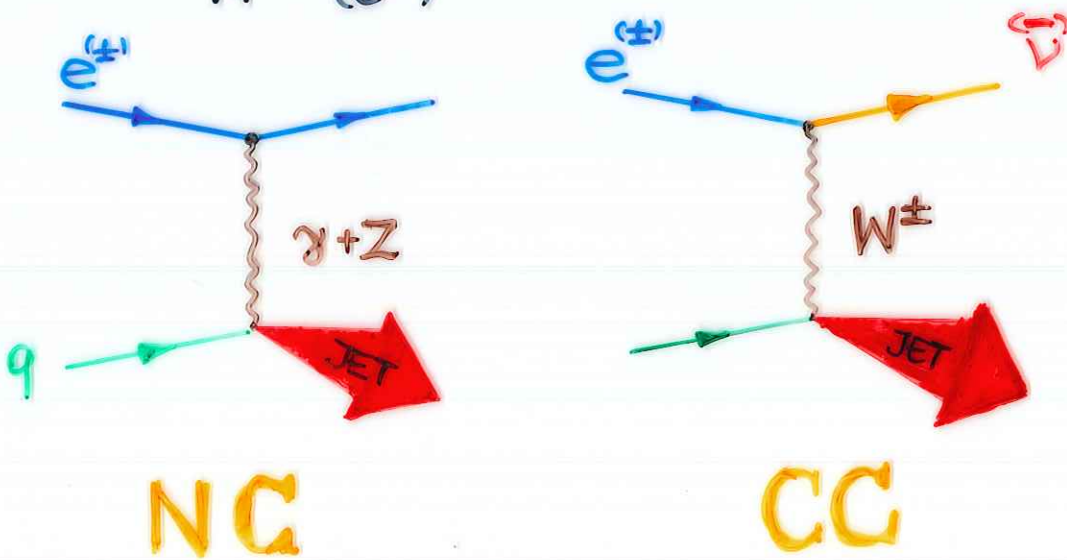
$$\mathcal{L} = 1.5 \cdot 10^{31} \text{ cm}^{-2} \text{ sec}^{-1}$$

$200 \text{ pb}^{-1} \sim 150$  fully efficient days.

$$Q^2 : 10 \dots 30\,000 \text{ GeV}^2$$

$$x : 10^{-4} \dots 0.8$$

$$y : \begin{matrix} .03 & (\text{jet}) \\ .1 & (e^{\pm}) \end{matrix} \dots 1.$$



POLARIZATION (LATER)  $\lambda = \pm .8$

2.

## BASIC RELATIONS

→ MEASURE :  $\frac{d^2\sigma_{NC}}{dx dQ^2}(e^\pm p)$  ;  $\frac{d^2\sigma_{CC}}{dx dQ^2}(e^\pm p)$   
 (+ USE  $\lambda \neq 0$  too!)

$$d\sigma_i^2 = d\sigma_i^{\text{BORN}} + d\sigma_i^{\text{1LOOP}}$$

↑  
QED dominated

THE STRUCTURE OF THE BORN CROSS SECTIONS:

$$\frac{d^2\sigma_{NC}^\pm}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left\{ \begin{array}{l} \gamma^2 \quad \gamma\bar{z} \quad z^2 \\ Y_+ [ F_2 + C_1 k E_2 + C_2 k^2 H_2 ] + \\ Y_- [ C_3 k X E_3 + C_4 k^2 X H_3 ] \end{array} \right\}$$

$$\frac{d^2\sigma_{CC}^{(\pm)}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left\{ \frac{1}{\alpha^2} \frac{g^2}{16\pi^2} \frac{Q^2}{Q^2 + M_W^2} \right\}^2 \frac{1 \mp \lambda}{2} \cdot \left\{ Y_+ W_{2,(\pm)}^{(\pm)} ; Y_- W_{3,(\pm)}^{(\pm)} \right\}$$

$$Y_+ = 1 + (1-y)^2 - \frac{Ry^2}{R+1} \quad ; \quad Y_- = 1 - (1-y)^2.$$

$$C_i = C_i(v_j, a_j, \lambda)$$

## STRUCTURE FUNCTIONS:

NC:

$$[F_2, G_2, H_2] = x \Sigma(q + \bar{q}) [Q_q^2, 2Q_q v_q, v_q^2 + a_q^2]$$

$$[xG_3, xH_3] = 2x \Sigma(q - \bar{q}) [Q_q a_q, v_q a_q]$$

CC:

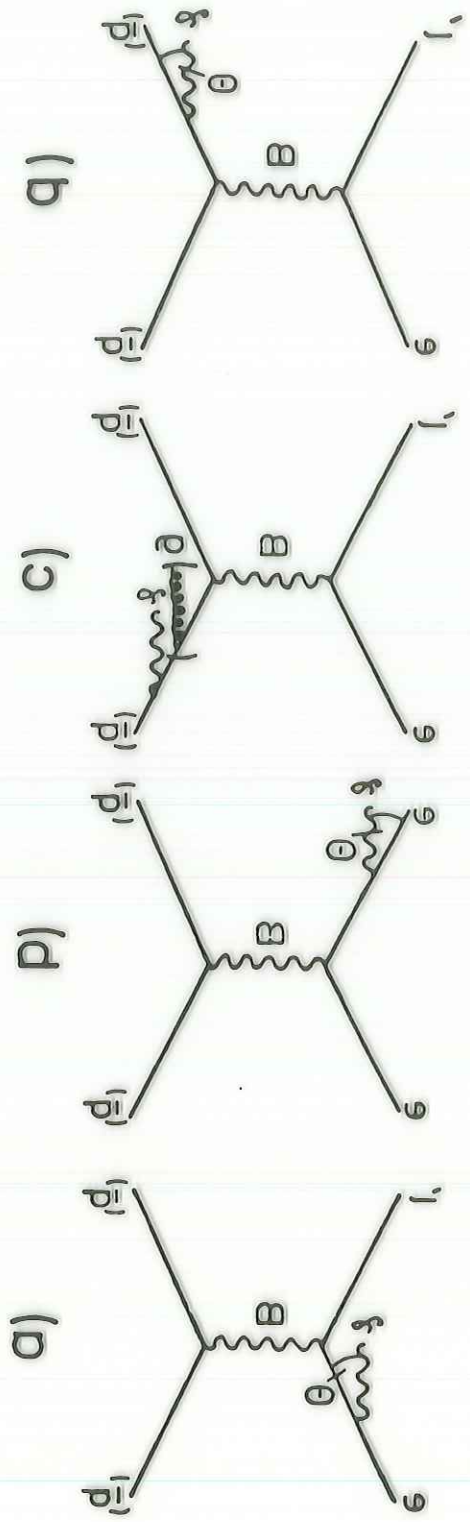
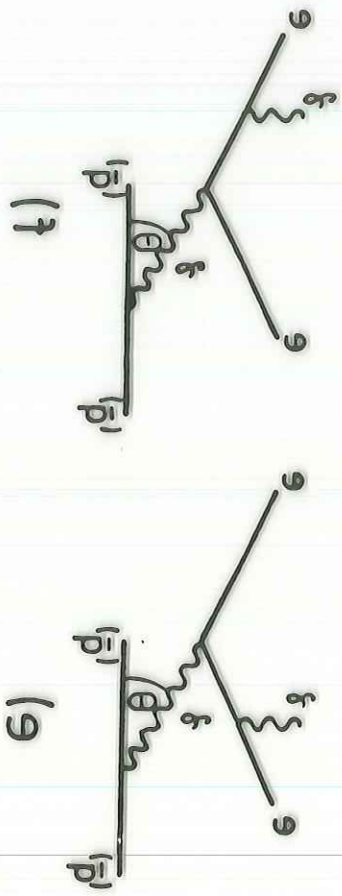
$$[W_2^-, xW_3^-] = [x \Sigma q_u + q_{\bar{d}}, x \Sigma q_u - q_{\bar{d}}]$$

$$[W_2^+, xW_3^+] = [x \Sigma q_d + q_{\bar{u}}, x \Sigma q_d - q_{\bar{u}}]$$

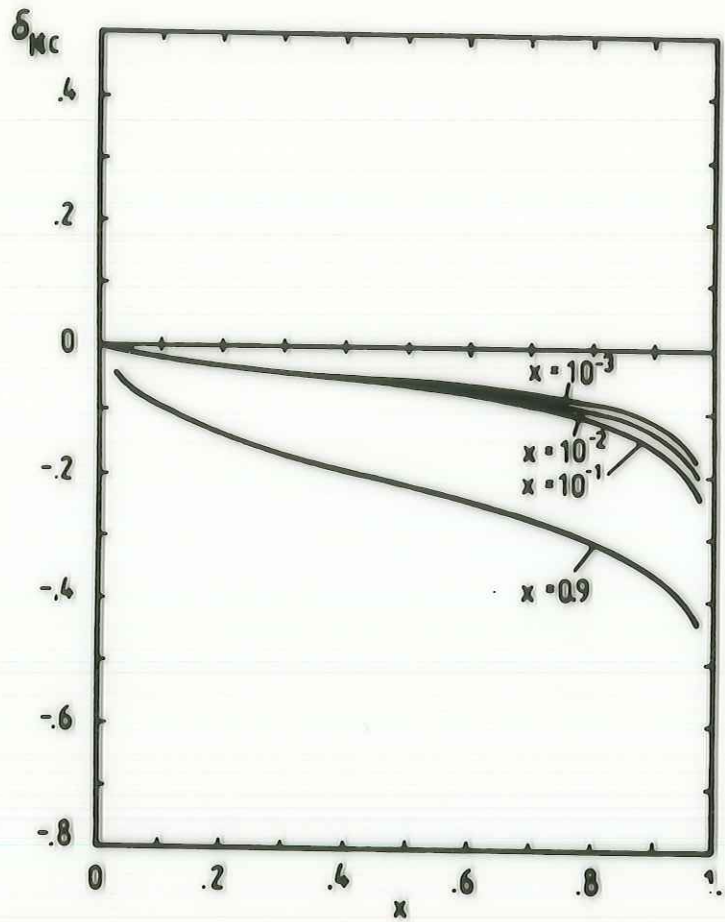
## COUPLINGS:

$$v_i = I_{3i}^L - 2Q_i \sin^2 \theta_w$$

$$a_i = I_{3i}^L$$







JET -  
MEASUREMENT

Fig. 2a

JET-MEASUREMENT

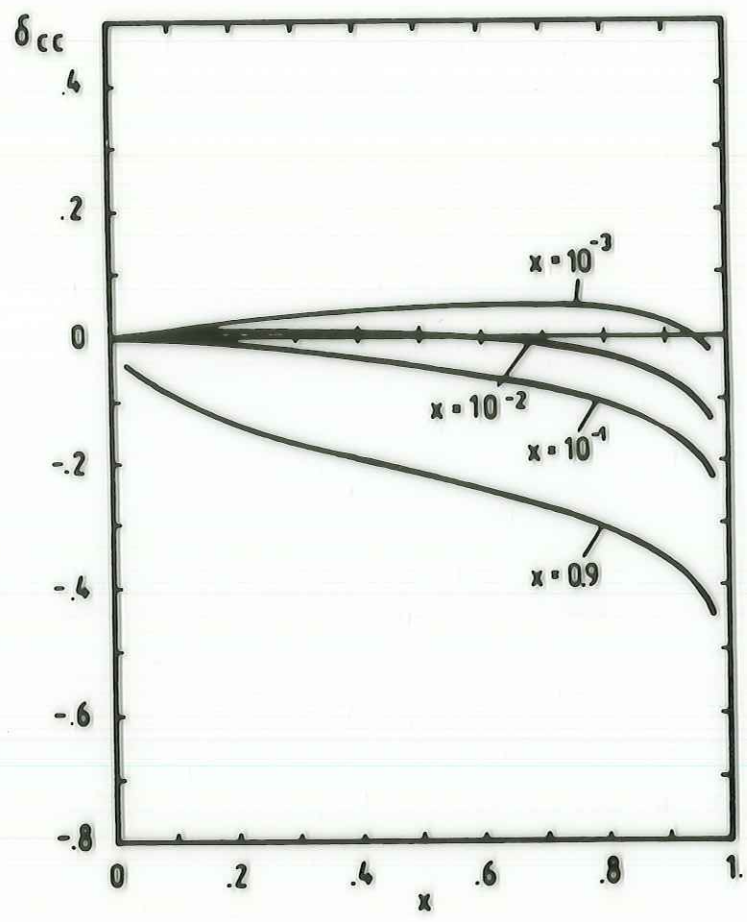


Fig.2b

WHAT DO WE FIX, WHAT WILL BE FITTED ?

ELECTROWEAK PARAMETERS :

$$\alpha, g, G_F, M_W, M_Z, \sin^2 \theta_W$$

ONLY 3 PARAMETERS ARE INDEPENDENT.

RELATIONS (+ RC) :

•• TREE :

$$\sin^2 \theta_W = 1 - M_W^2 / M_Z^2$$

$$g^2 = 4\pi \alpha / \sin^2 \theta_W$$

$$G_F = g^2 \sqrt{2} / 8M_W^2 (1 - \Delta r)^{1/2}$$

↳  $f(m_t, m_H)$

$$K_Z(Q^2) = \frac{Q^2}{Q^2 + M_Z^2} \frac{1}{4s_\theta^2 c_\theta^2}$$

or :

$$K_W(Q^2) = \frac{G_F M_W^2}{2\sqrt{2} \alpha} \frac{Q^2}{Q^2 + M_W^2} (1 - \Delta r)^{1/2}$$

$$K_Z(Q^2) = \frac{G_F M_Z^2}{2\sqrt{2} \alpha} \frac{Q^2}{Q^2 + M_Z^2} (1 - \Delta r)^{1/2} \dots$$

→ SYSTEMATIC SEARCH FOR SENSITIVITIES

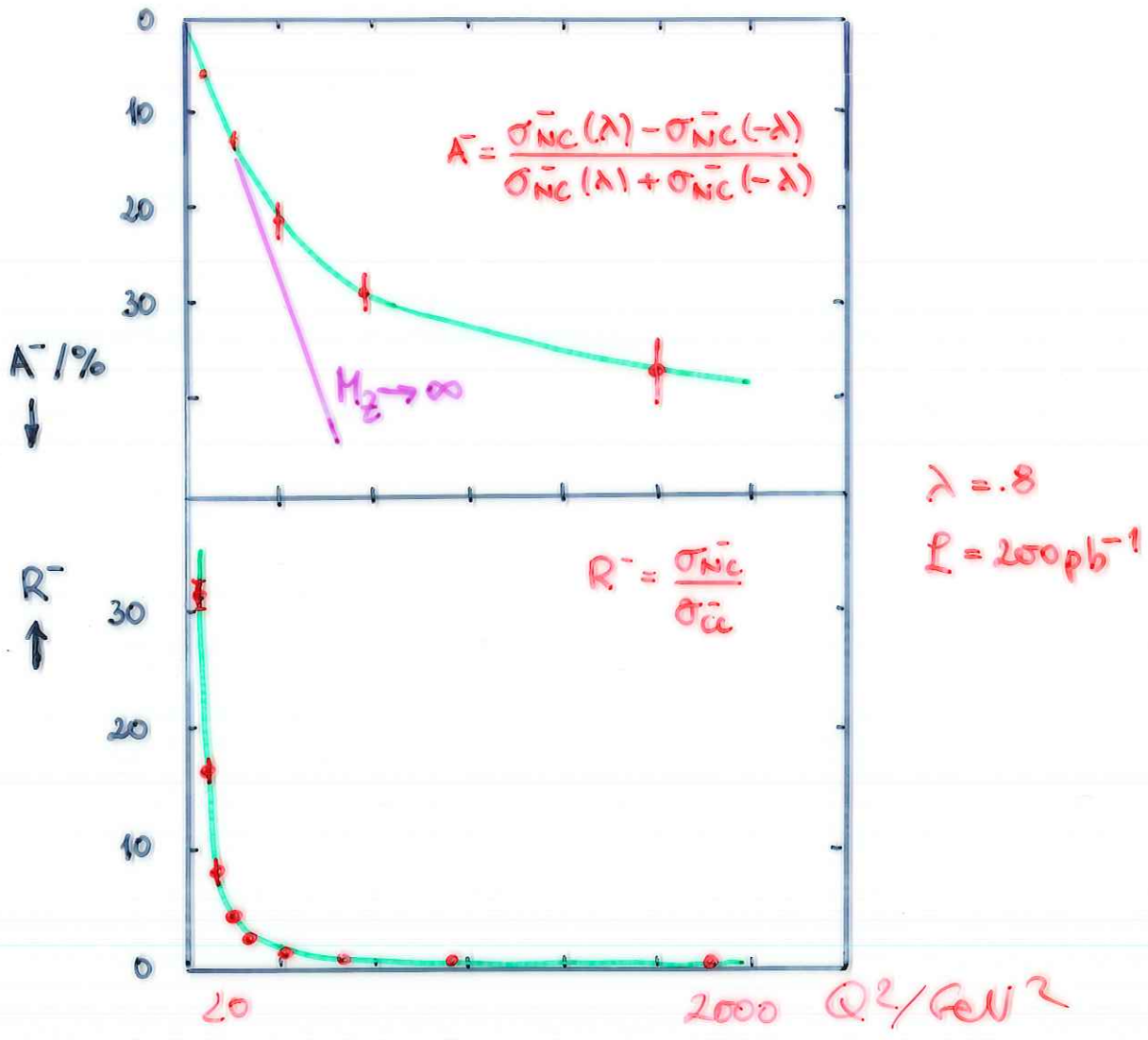
REQUIRED :

- OBSERVABLES

- PARAMETERS (fitting, fixing)



### 3. STATISTICAL PRECISIONS



SENSITIVITY OF EW-PARAMETERS  
FIXING  $G_p, M_Z$

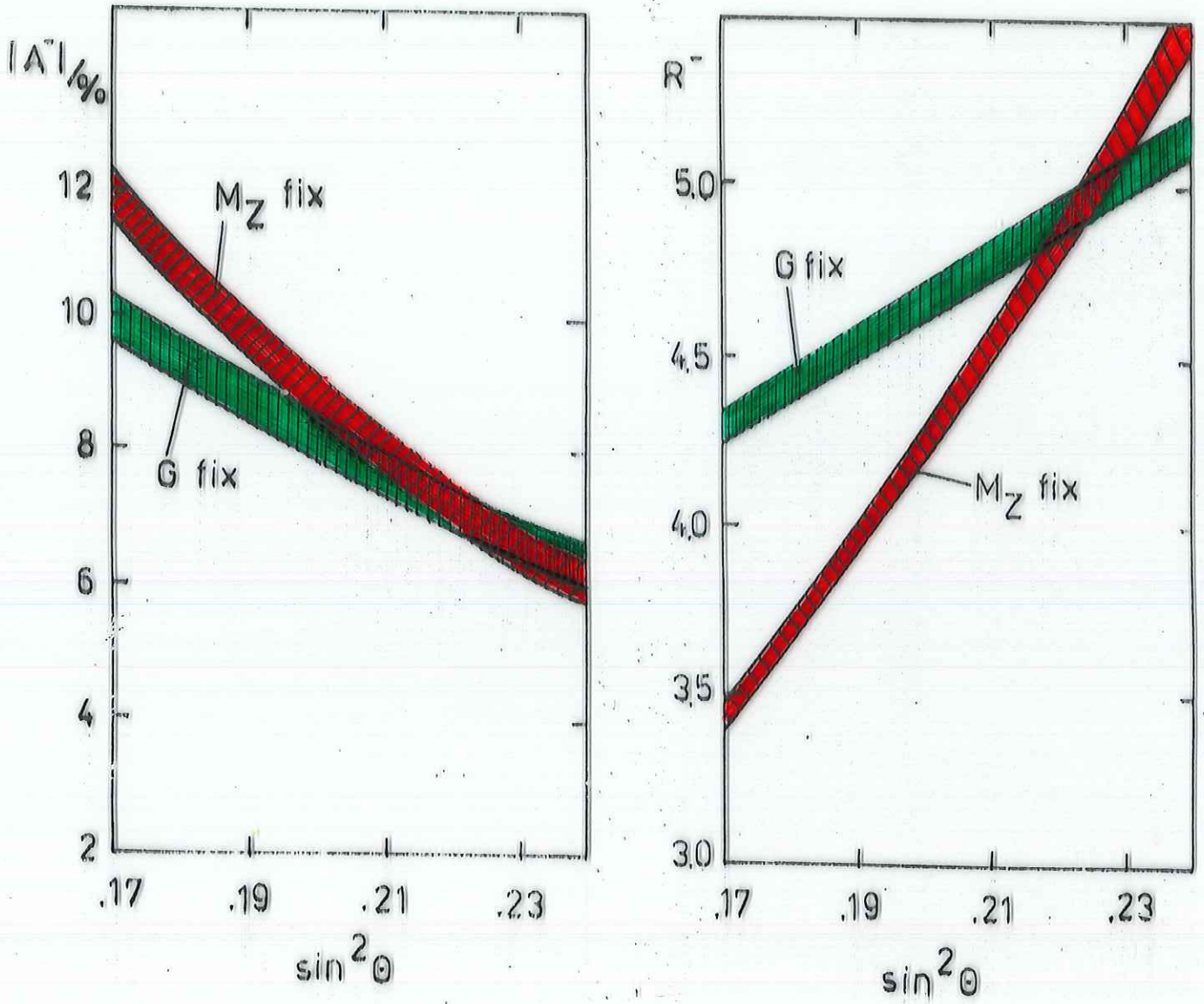


Fig. 2

$$\sin^2 \theta = 1 - \frac{M_W^2}{M_Z^2}$$

CUT-DEPENDENCE OF  
THE STATISTICAL SENSITIVITY :

$A^-$  AND  $R^-$

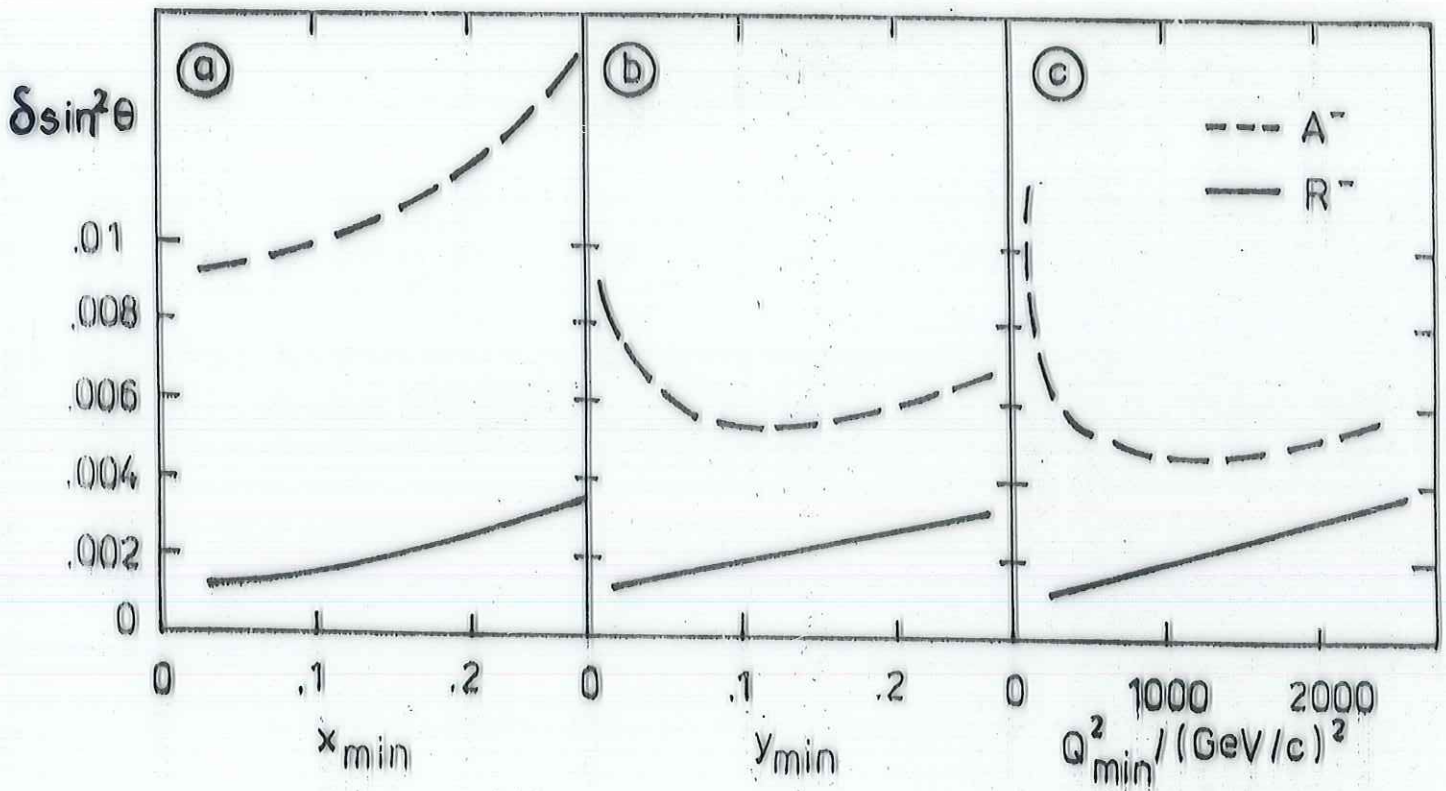
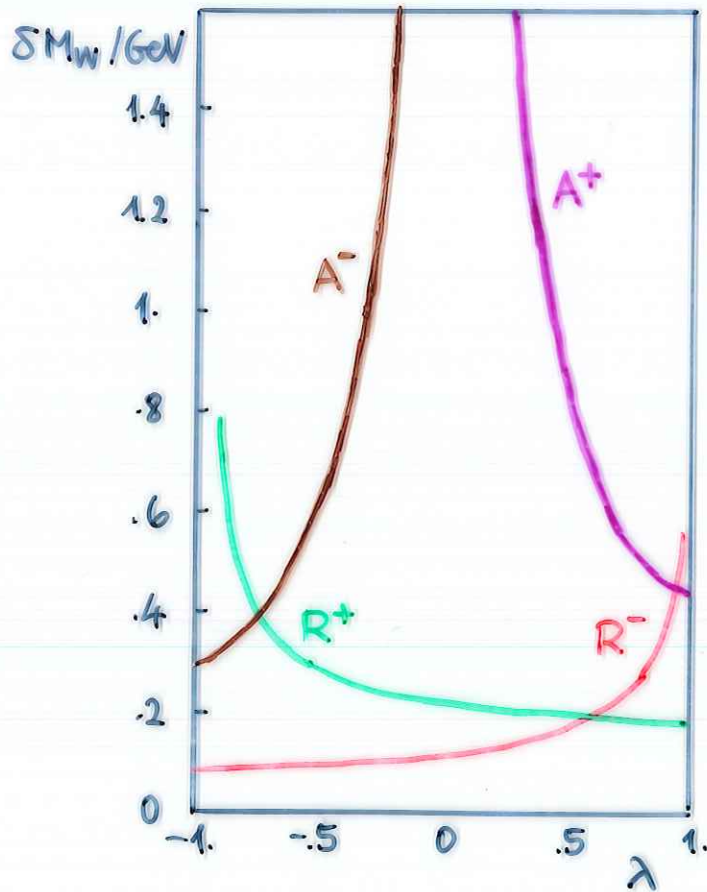


Fig. 3

$\mathcal{L} = 200 \text{ pb}^{-1}$

FINAL CUTS :  $x > .1$   
 $y > .1$   
 $Q^2 > 500 \text{ GeV}^2$

# POLARIZATION: IS IT NEEDED ?!





# STATISTICAL PRECISIONS

fixed error		$S_\theta^2$	$M_z$	$M_W$	$G_F$
$\Delta S_\theta^2$	A <sup>-</sup>		.005	.005	.007
	R <sup>-</sup>		.002	.002	.005
$\Delta M_z / \text{GeV}$	A <sup>-</sup>	3.02		.25	1.09
	R <sup>-</sup>	.51		.10	.76
$\Delta M_W / \text{GeV}$	A <sup>-</sup>	2.53	.27		1.38
	R <sup>-</sup>	.45	.10		.95

$\alpha$

$\lambda = .8$

INFLUENCE OF THE ERROR OF THE FIXED QUANTITY ON THE VALUE OF THE FITTED

(EW-  
INPUT  
UNCERTA

fixed Fixed	$\Delta \sin^2 \theta$		$\Delta M_z / \text{GeV}$		$\Delta M_W / \text{GeV}$	
	A <sup>-</sup>	R <sup>-</sup>	A <sup>-</sup>	R <sup>-</sup>	A <sup>-</sup>	R <sup>-</sup>
$\Delta S_\theta^2$ = ±.001			- .58 + .57	± .26	- .54 + .53	± .28
$\Delta M_z$ = ± 50 MeV	± .0001	± .0002			+ .05 - .04	± .05
$\Delta M_W$ = ± 50 MeV	± .0001	± .0002	+ .04 - .04	± .05		



## 4. SYSTEMATIC EFFECTS

UNCERTAINTIES OF PARTON DISTRIBUTIONS:  $x > .1$

$\delta S_0^2$	SEA	$x_{uv}$	$x_{dv}$
$A^-$	$\mp .0003$	$\mp .0014$	$\pm .0011$
$R^-$	$\pm .0017$	$\pm .0031$	$\pm .0015$

● CALLEN-GROSS RELATION:

SHIFT  $R=0 \rightarrow R=.1$

$$\delta S_0^2 = .0003 \text{ (.0008)} \quad A^- (R^-)$$

● SWITCHING  $m_Q$  ON AND OFF

$$m_c = 1.25 \text{ GeV}, \quad m_b = 4.5 \text{ GeV}, \quad m_t = 40 \text{ GeV}$$

$$\delta S_0^2 = .0001 \quad R^- \text{ even smaller for } A^-$$

## 5. EXTENSIONS OF THE MODEL

GIVE UP:

-  $g = (M_W / M_Z \cos\theta)^2 = 1$

Fig.

-  $v = I_3^L - I_3^R - 2Q \sin^2\theta$        $I_3^R \neq 0$   
 $a = I_3^L - I_3^R$

- Decouple the W-propagator from the other electroweak parameters

$\delta I_3^R$	:	e	u	d	
		.056	.016	.034	A <sup>-</sup>
		.030			A <sup>+</sup> !

$\delta M_W^{\text{loop}} \approx 400 \text{ MeV}$  , R<sup>-</sup>.

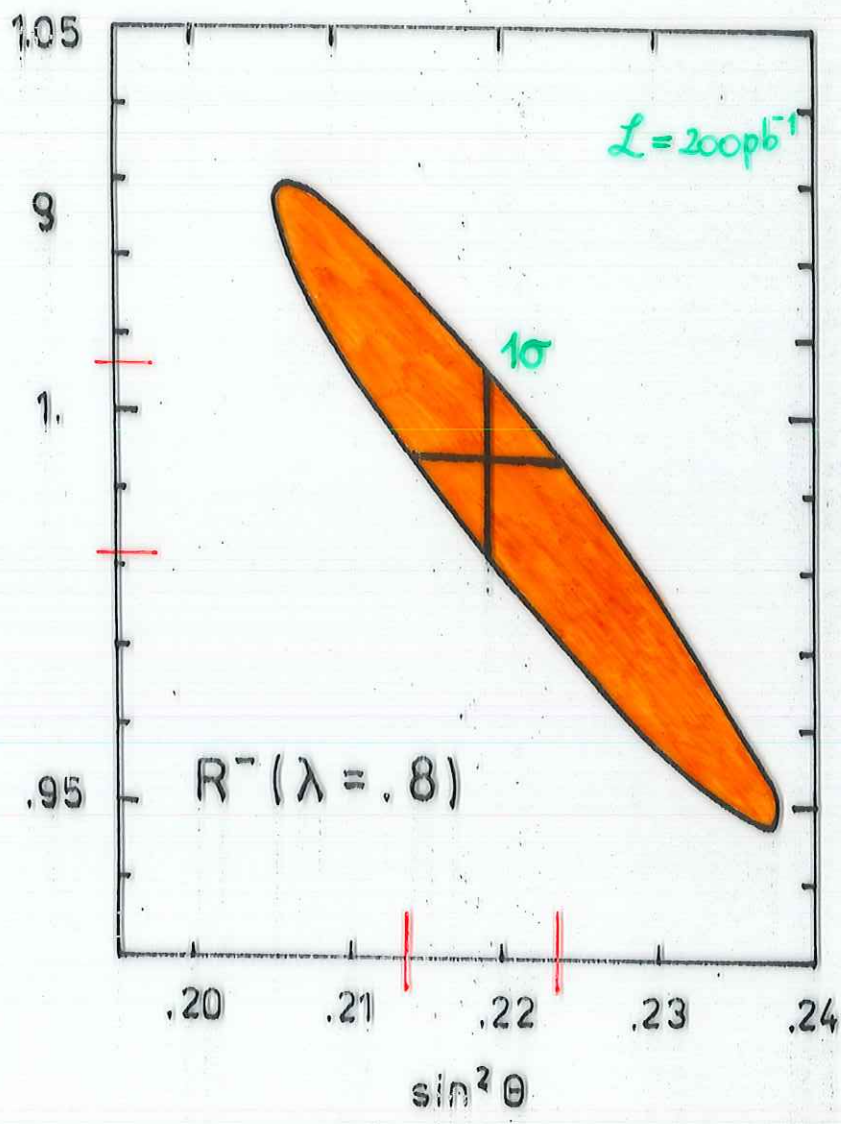


Fig. 8



6.

SENSITIVITY ON ADDITIONAL GAUGE BOSONS

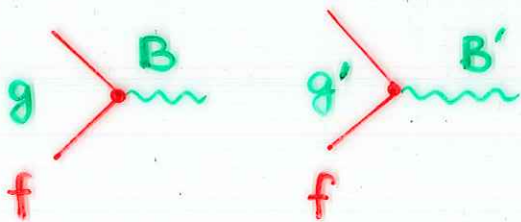
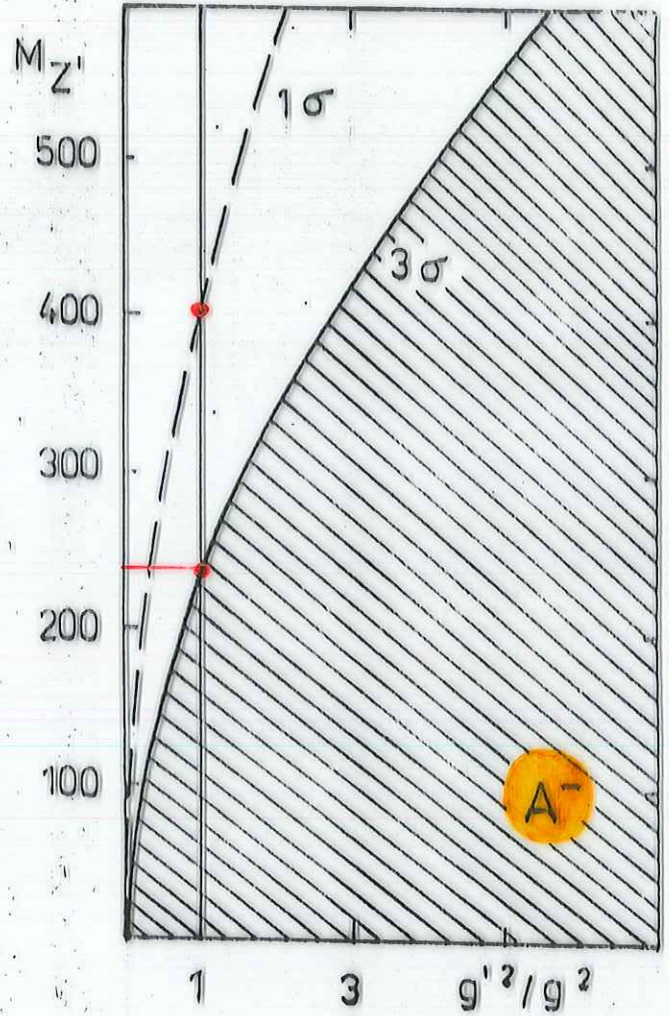
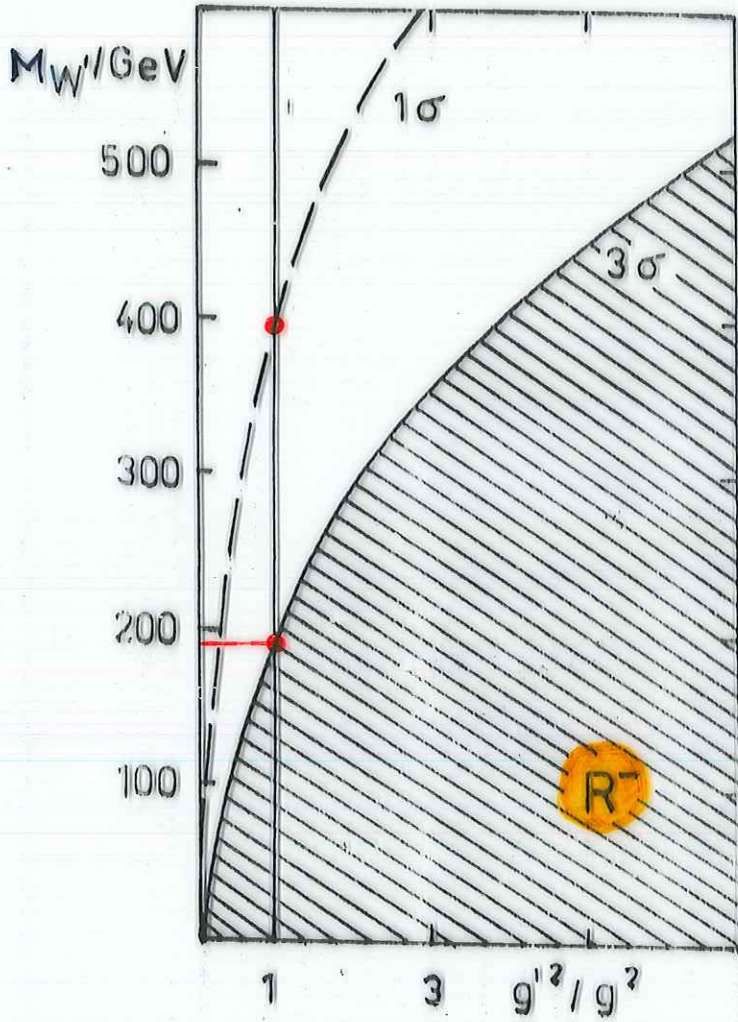
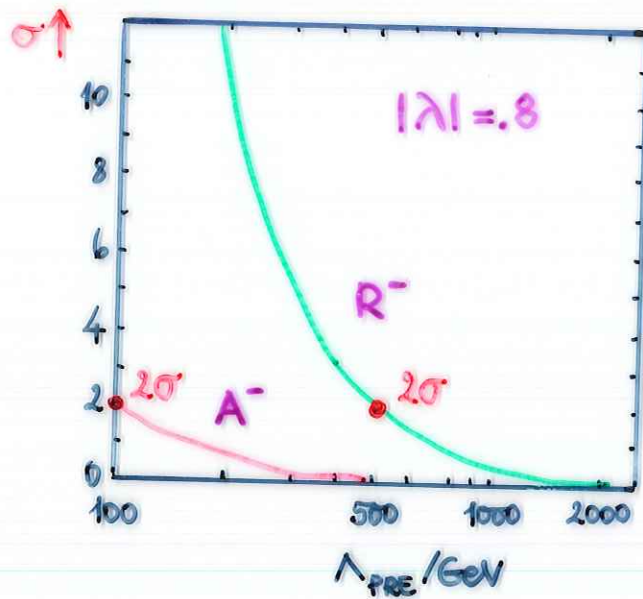


Fig. 9

$x > 0.1, y > .01, Q^2 > 500 \text{ GeV}^2, \mathcal{L} = 200 \text{ pb}^{-1}$

COMPOSITENESS SCALE:  
W's & Z's



$$K_{E,N}(Q^2) = \frac{Q^2}{Q^2 + M^2} \cdot A \cdot \frac{1}{1 + \frac{Q^2}{\Lambda_{PRE}^2}}$$



# 7. CONCLUSIONS

- BEST PRECISIONS: Fix  $\alpha, M_Z$ : FIT A THIRD PARAMETER

$$\begin{array}{l}
 L = 200 \text{ pb}^{-1} \\
 R^-
 \end{array}
 : \begin{array}{l}
 \begin{array}{l}
 \text{stat} \quad \text{sys} \\
 \pm 100 \text{ MeV} \pm 100 \text{ MeV} \\
 \text{stat.} \quad \text{sys} \\
 \pm .002 \pm .002
 \end{array}
 \delta M_W \\
 \delta S_0^2
 \end{array}
 \left. \vphantom{\begin{array}{l} L \\ R^- \end{array}} \right\} SU_{2L} \times U_{1Y}$$

$x > .1, y > .1, Q^2 > 500 \text{ GeV}^2$

$A^-$ : 2...3 TIMES WORSE EVEN AT  $|\lambda| = .8$  (statistics)

- $R^-$  PRECISIONS DEPEND ONLY WEAKLY ON  $\lambda$ .  $\lambda = 0$  INTRODUCES A FACTOR OF  $\approx 1.2$  ON  $\delta S_0^2$  etc.

- MAIN SYSTEMATIC EFFECTS:

UNCERTAINTIES IN  $x_s, x_{uv}, x_{dv}$

$\sim \delta \rightarrow O(\delta_{\text{stat}})$ .

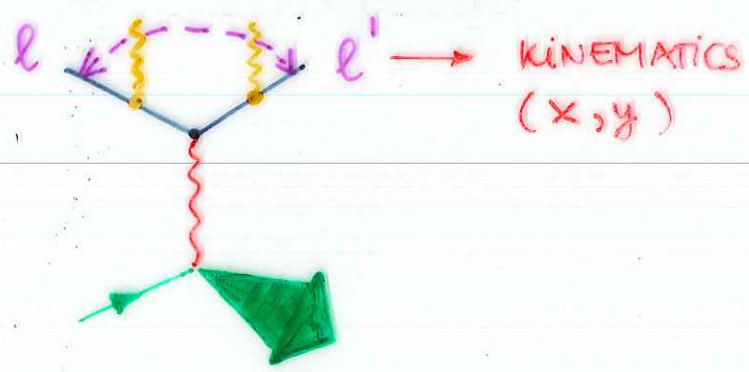
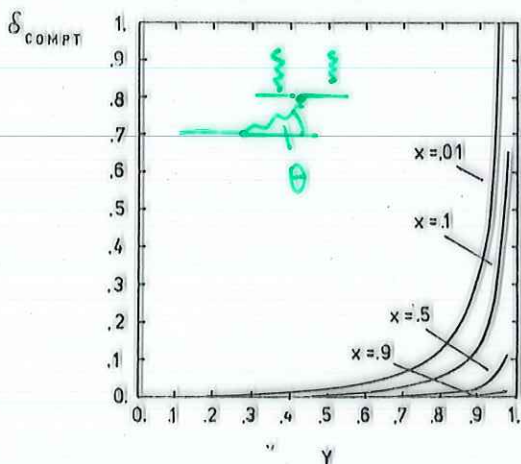
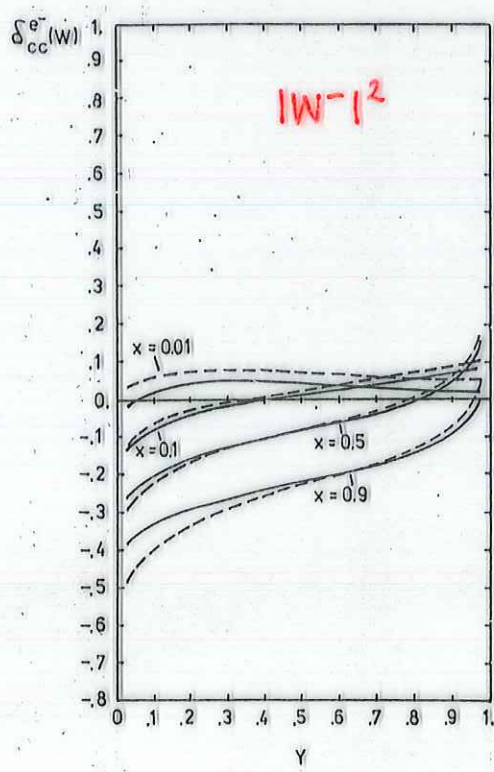
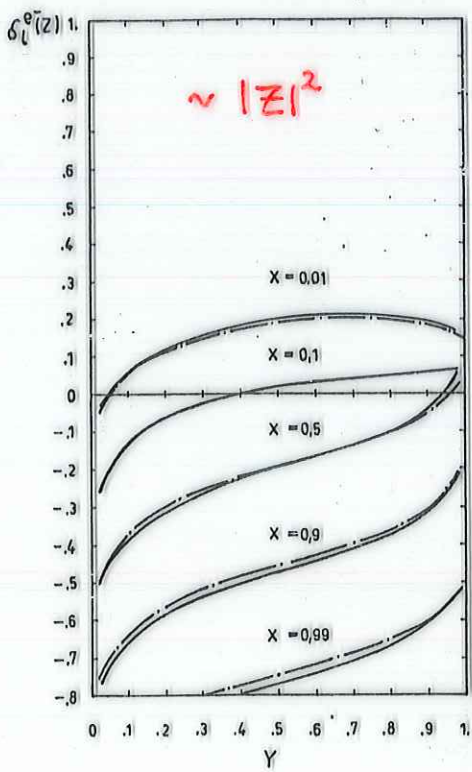
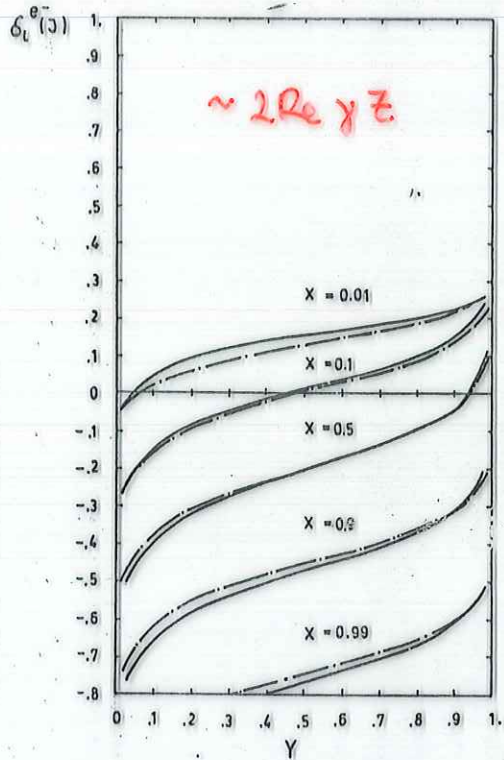
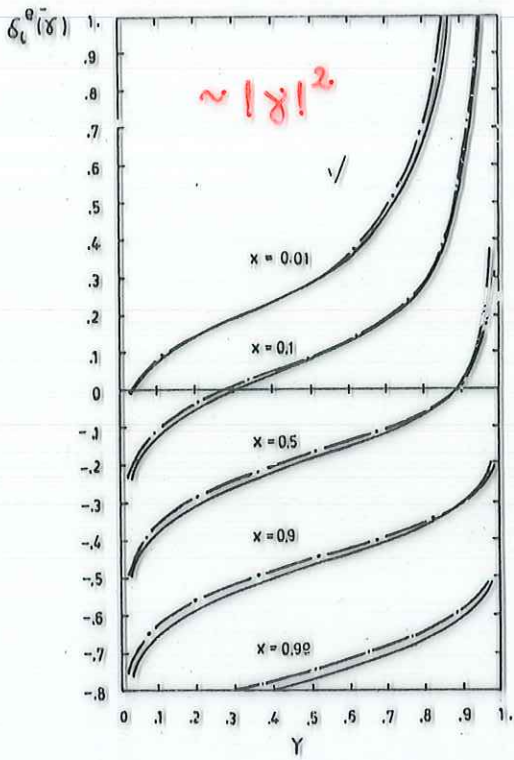
OTHER UNCERTAINTIES: EW INPUT

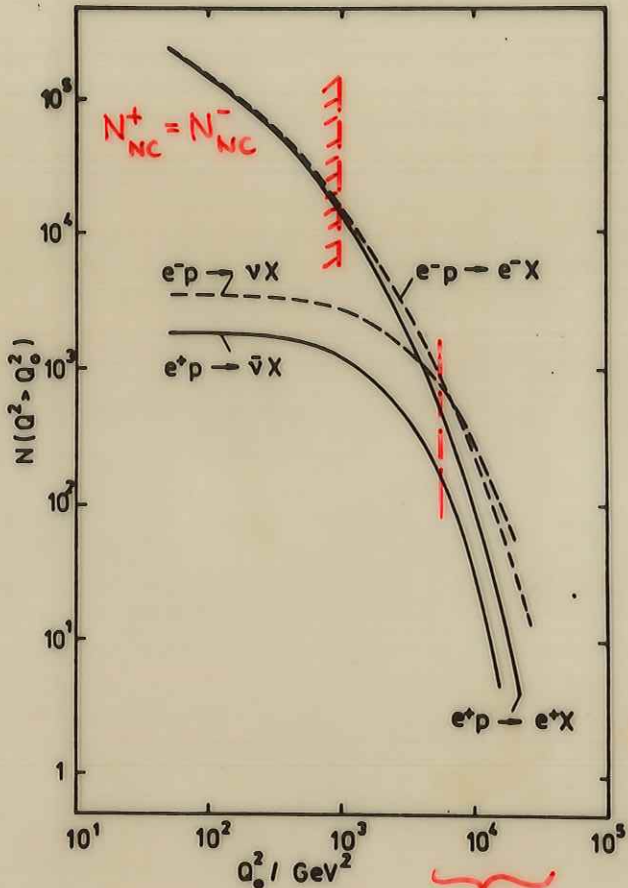
$\sigma_L/\sigma_T, m_q$  LESS IMPORTANT

- $\delta g_{\text{stat}} = \pm .003$   $R^-$   $\delta M_W = 400 \text{ MeV}$   $R^-$   
 $\delta I_{\text{re}}^3 = \pm .03$   $A^+$  (propagator only)

- $M_Z'$   $3\sigma$  ( $1\sigma$ )  $230$  ( $400 \text{ GeV}$ )
- $M_W'$   $3\sigma$  ( $1\sigma$ )  $190$  ( $390 \text{ GeV}$ )

- $\Lambda_{\text{PRE}}(W, Z)$ :  $2\sigma$   $A^-$   $100 \text{ GeV}$   
 $R^-$   $500 \text{ GeV}$





EVENT RATES FOR  $Q^2 > Q_0^2$ :

$x > .01, y > .03$   
 $\mathcal{L} = 100 \text{ pb}^{-1}$

UNFOLDING OF QUARK DISTRIBUTIONS  
 ELECTROWEAK TESTS ←

